

Rebalancing Idle Vehicles via Distributed Coverage Control in Mobility-on-Demand systems

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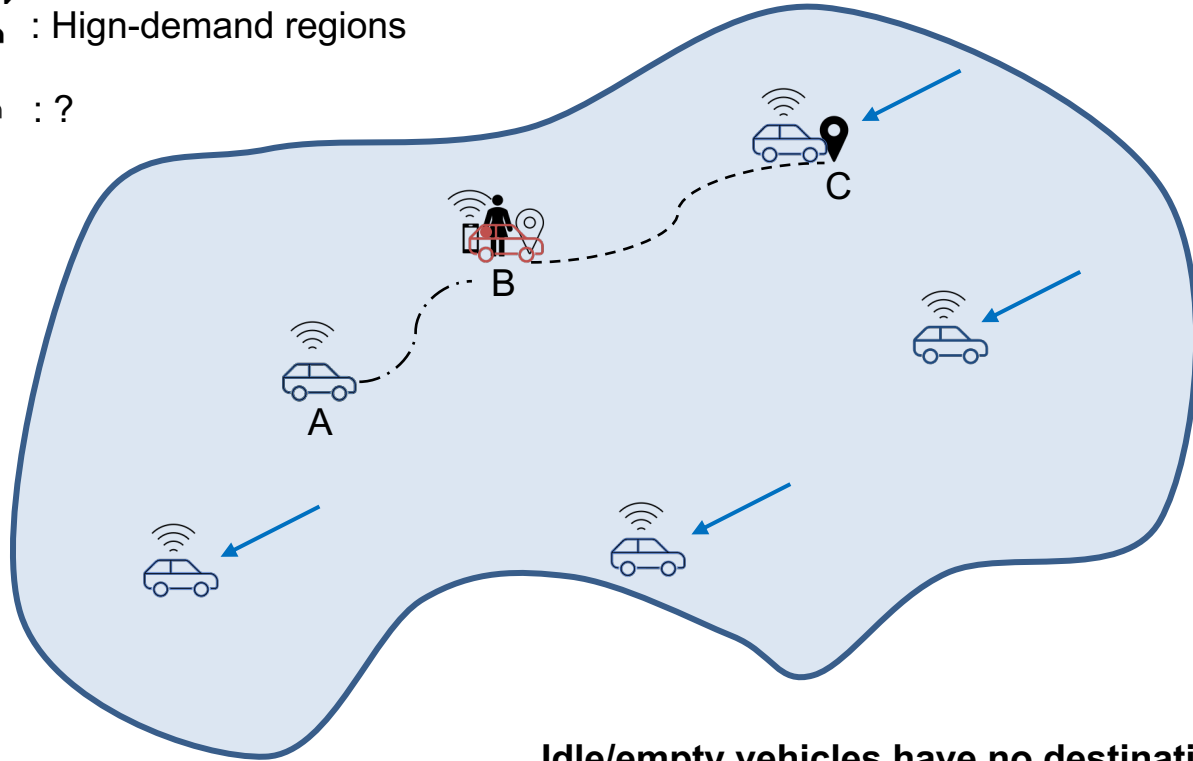
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  : High-demand regions

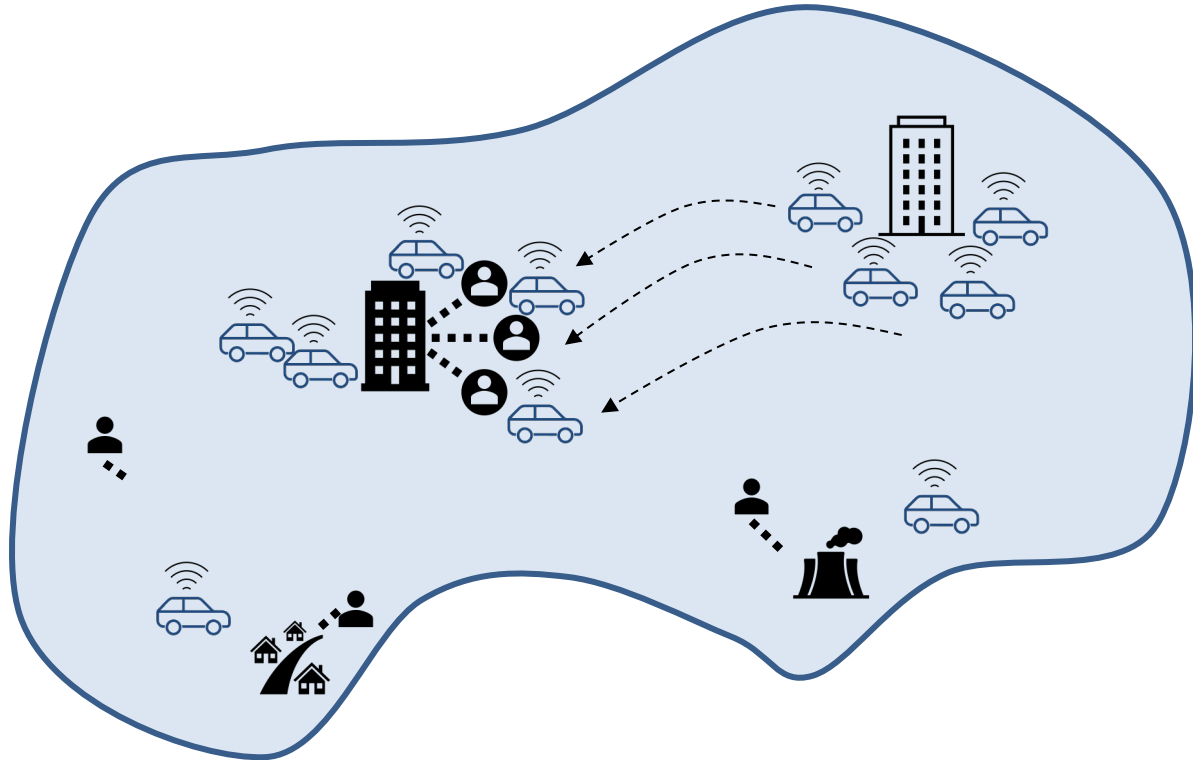
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**Idle/empty vehicles have no destinations.
Where should they go?**

Imbalance in the spatial distribution of vehicles:

- Non-uniform passenger's demand for rides in different districts
- Asymmetry between origin and destination distributions of trips



Goal: rebalancing vehicles

- Relocating idle/empty vehicles to the high-demand regions

Vehicle rebalancing problem

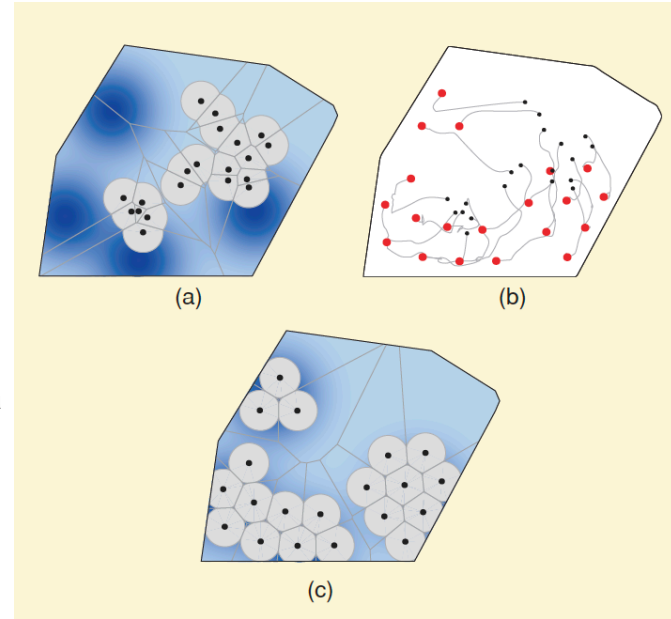
Coverage control problem:

Every agent/vehicle is responsible for covering a certain area

$$H(X, W) = \sum_{i=1}^n H(x_i, W_i') = \sum_{i=1}^n \int_{q \in W_i'} f(\|x_i - q\|^2) \varphi(q) dq$$

$\varphi(q)$: demand density function,

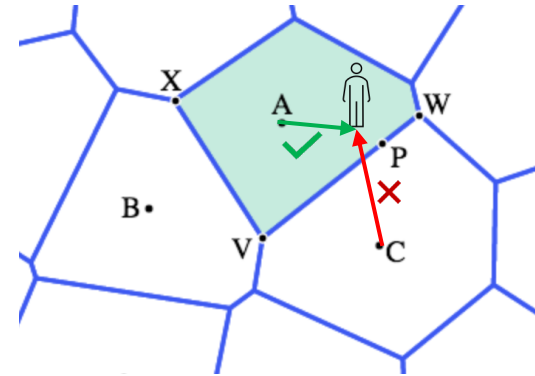
$f: [0, \infty) \rightarrow \mathcal{R}$, a performance function which degrades with distance.



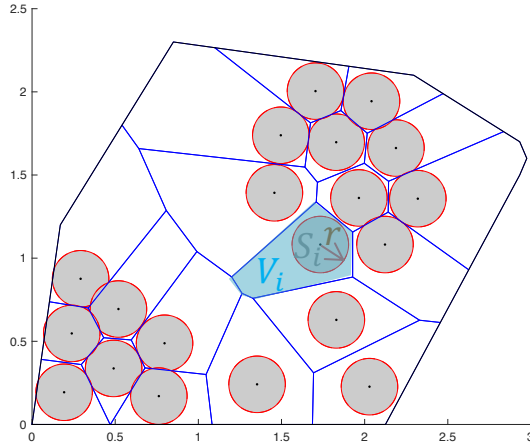
Problem Formulation

Voronoi partition:

- The partitioning of a plane with n points into convex polygons
 - Each cell contains one generator/seed
 - Every point in a given cell is closer to its seed than to any other
-
- With Voronoi diagram, we can disperse the vehicles in the region



Coverage Control Algorithm



Important variables :

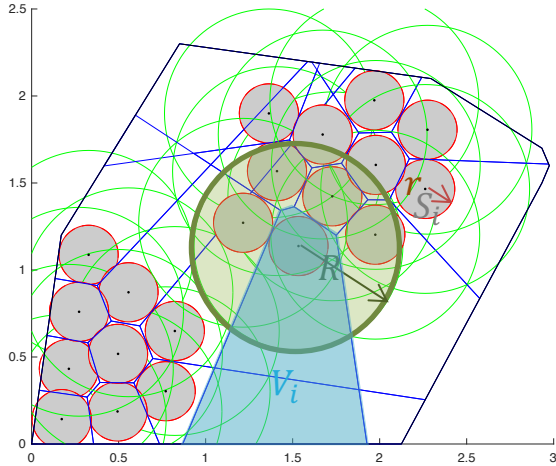
- N = Number of agents
- r = Agent coverage radius

Objective :

Maximize the value of H

$$H(X, W) = \sum_{i=1}^n H(x_i, W_i) = \sum_{i=1}^n \int_{q \in W_i} f(\|x_i - q\|^2) \varphi(q) dq$$
$$W_i = S_i \cap V_i$$

Distributed Coverage Control Algorithm



Important variables :

- N = Number of agents
- r = Agent coverage radius
- R = Agent communication limitation radius

Objective :

Maximize the value of H

$$H(X, W') = \sum_{i=1}^n H(x_i, W'_i) = \sum_{i=1}^n \int_{q \in W'_i} f(\|x_i - q\|^2) \varphi(q) dq$$
$$W'_i = S_i \cap V'_i$$

Distributed Coverage Control Algorithm

Proposition: The local maximum of H can be obtained when all x_i are located at centroids (centers of mass, $C_{W'_i}$) of their respective Voronoi cells (W'_i), i.e., **Centroidal Voronoi Configuration(CVC)**.

Distributed Control Law Formulation:

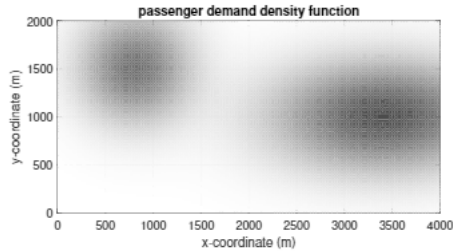
$$\frac{dx_i}{dt} = u_i, \quad \frac{\partial H}{\partial x_i} = -2M_{W'_i} \|x_i - C_{W'_i}\|,$$

$$\blacktriangleright \quad u_i = -k_p (x_i - C_{W'_i}),$$

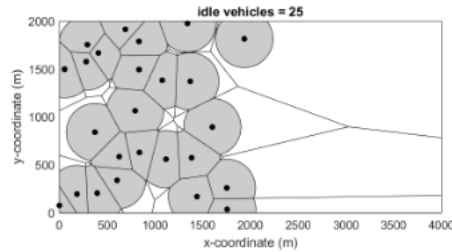
$$\frac{\partial H}{\partial t} = \sum_{i=1}^n \frac{\partial H}{\partial x_i} \frac{dx_i}{dt} = 2k_p \sum_{i=1}^n M_{W'_i} \|x_i - C_{W'_i}\|^2 > 0.$$

which steer the agent team to converge to CVC.

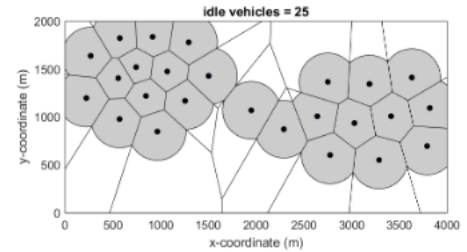
Case Study I: Continuous Case



(a) Demand density function

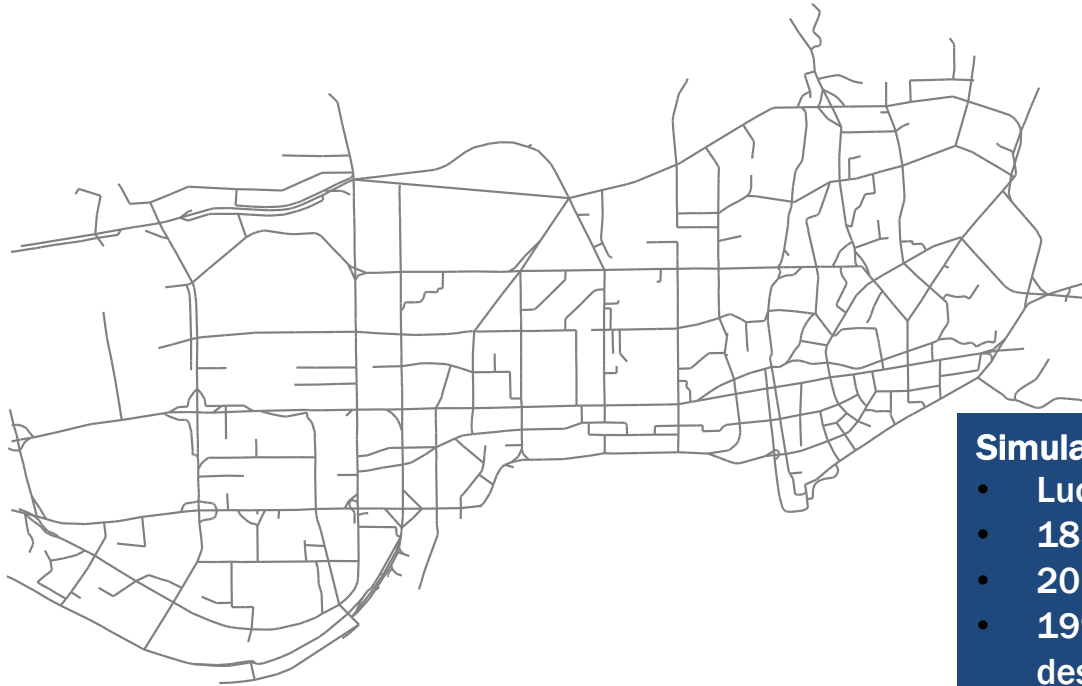


(b) Initial configuration



(c) Final configuration

Case Study I I : Shenzhen, China



Simulated network:

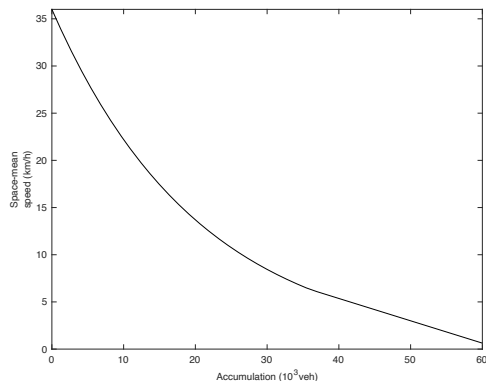
- Luohu District of Shenzhen, China
- 1858 nodes
- 2013 links
- 199,819 trips consisting of origins, destinations, and time

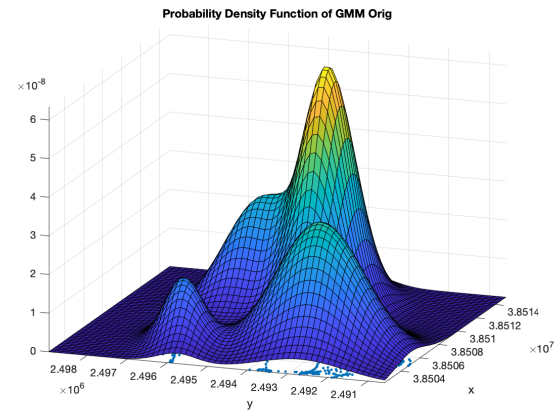
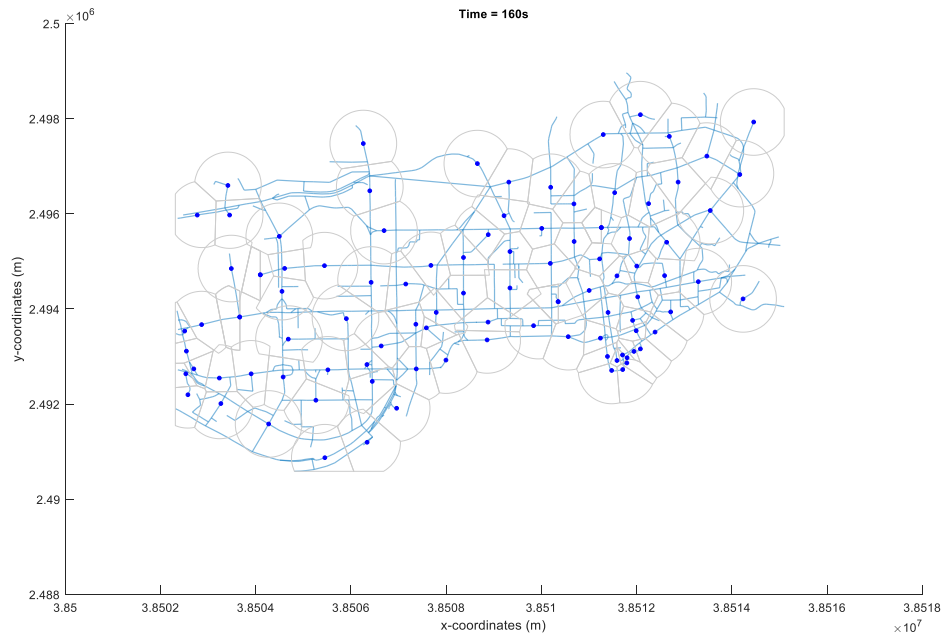
Experimental Setup

- 3-hour simulation
- Time Pattern of demand: low-high-low, each period lasts for 1 hour
- 2400 orders
- Fleet size = 100

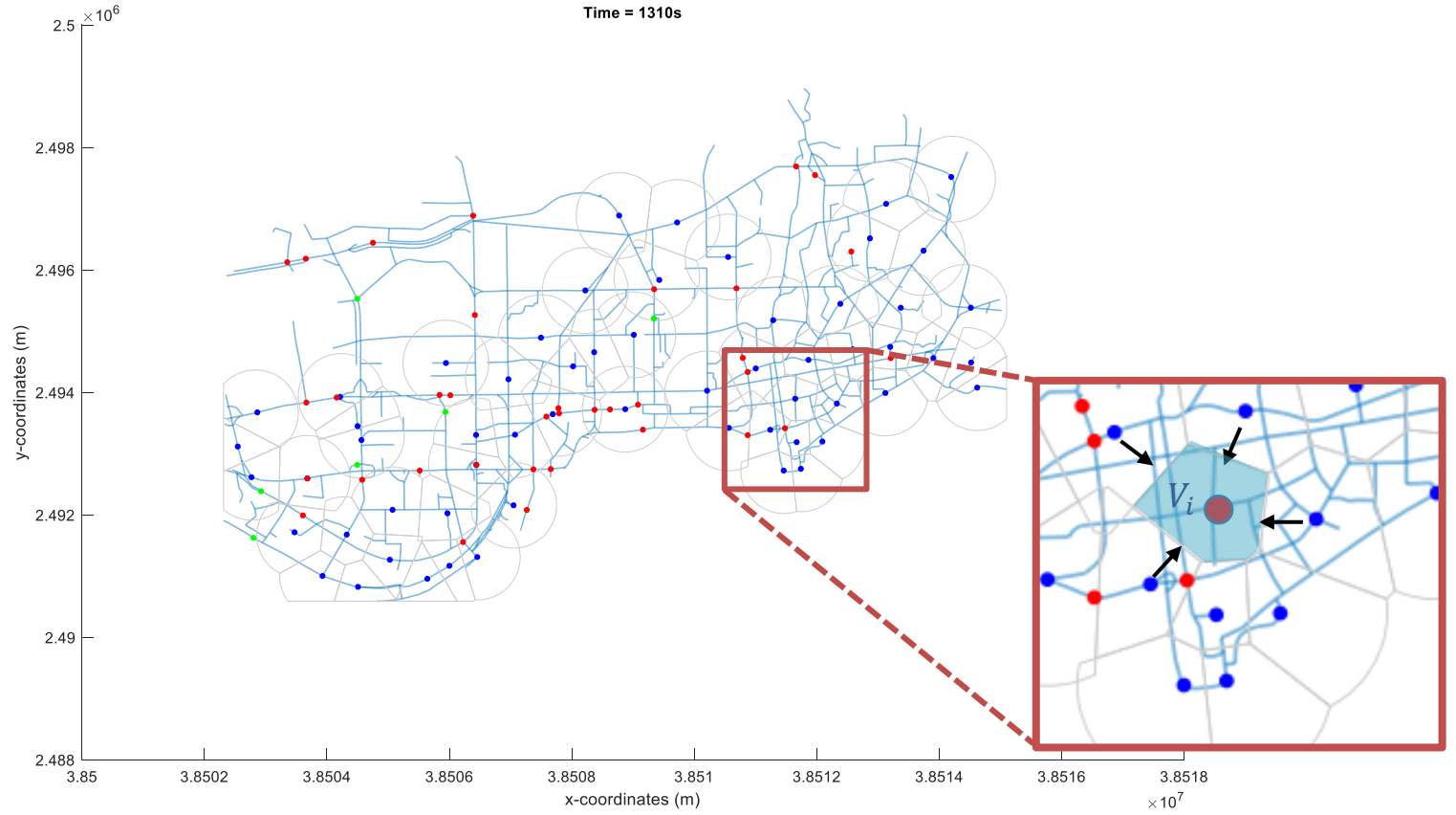
- Private vehicles; Ride-hailing vehicles
- macroscopic fundamental diagram (MFD) for Shenzhen

$$v(n) = \begin{cases} 36e^{\left(\frac{29m}{600}\right)}, & \text{if } m \leq 36, \\ 6.31 - 0.28(m - 36), & \text{if } 36 < m \leq 60, \\ 0, & \text{if } m > 60 \end{cases} \quad \text{where } m \equiv \frac{n}{1000}.$$



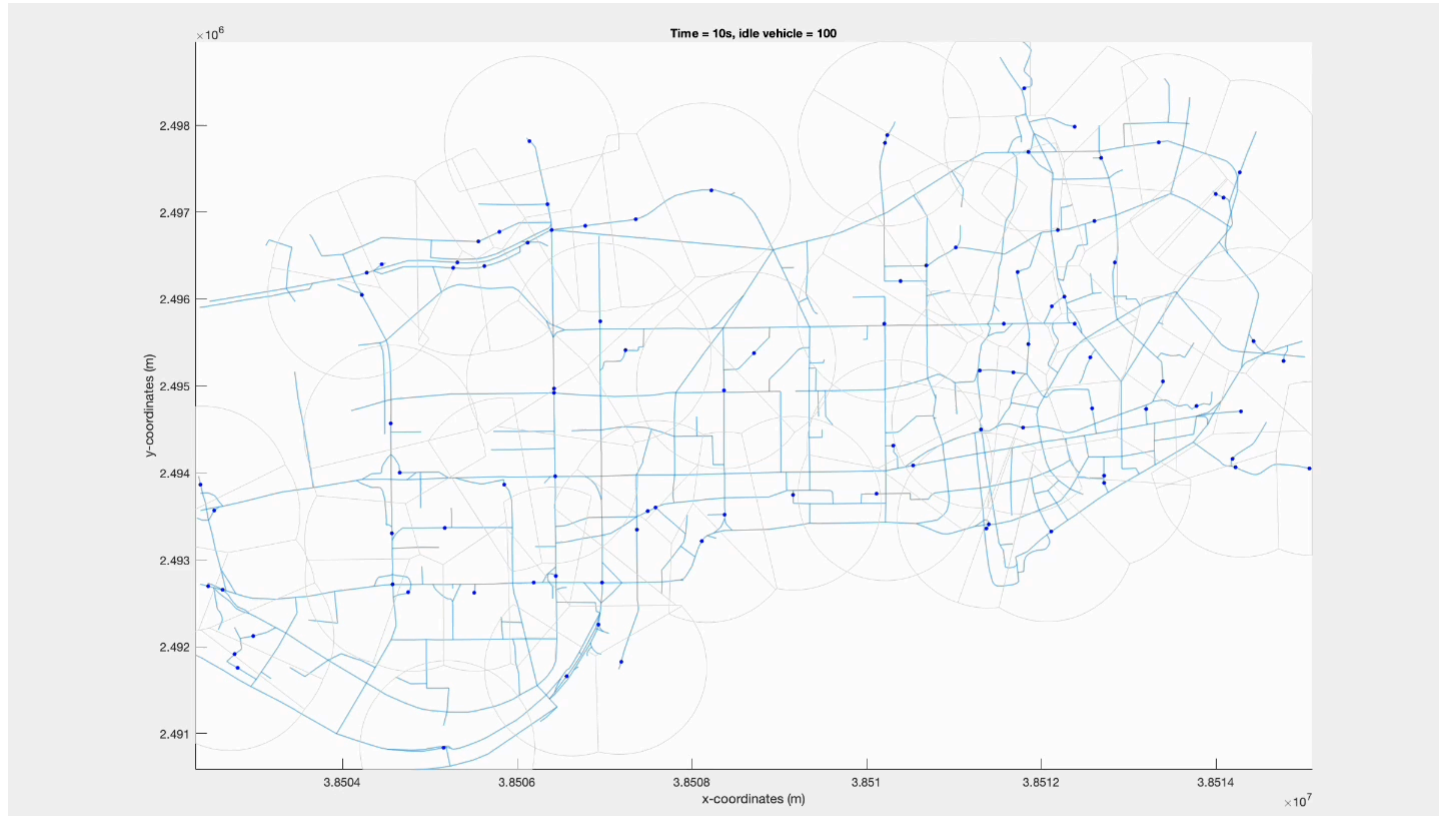


Real map: Shenzhen city



blue: idle vehicle (i.e., empty, looking for a passenger),
red: passenger-assigned vehicle,
green: passenger-carrying vehicle.

Demo video: Shenzhen city



blue: idle vehicle (i.e., empty, looking for a passenger),
red: passenger-assigned vehicle,
green: passenger-carrying vehicle.

Performance metrics

- Order completion rate: $\frac{N_1}{N} = \frac{N_1}{N_1 + N_2} \times 100\%$

- Average Waiting time: $t_w = \frac{\sum_{i=1}^{N_1} (t_p^r(i) - t_o(i))}{N_1}$

- Average System time(with penalty for cancelled orders):

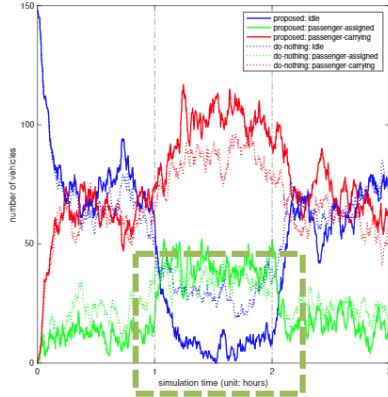
$$t_{sys} = \frac{\sum_{i=1}^{N_1} (t_p^r(i) - t_o(i)) + N_2 \cdot \alpha \cdot w_{tol}}{N}$$

$\alpha = 1.5, w_{tol} = 5 \text{ min}$

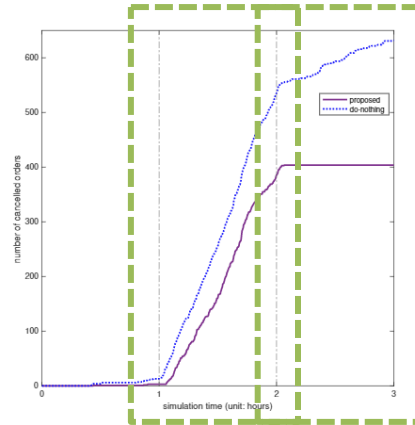
- 3-hour simulation
- Time Pattern of demand: low-high-low, each period lasts for 1 hour
- 2400 orders
- Fleet size = 150

	Proposed method	Do-nothing policy	Improvement
Completion rate(%)	82.9	73.2	13.3%↑
Average waiting time(s)	132.5	173.9	23.8%↓
Average system time(s)	186.8	247.9	24.6%↓

Fig : Comparison of different states of vehicles and number of canceled orders



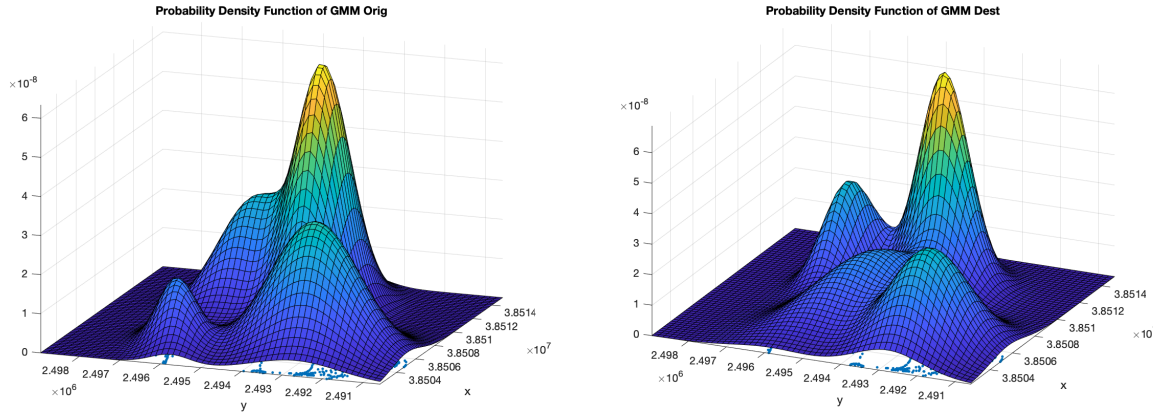
(a) Number of idle (blue), passenger-assigned (green), and passenger-carrying (red) vehicles



(b) Number of accumulated canceled orders

- Operate the fleet more efficiently as a larger amount of vehicles are actively serving passengers

Depict imbalance between the origin and destination distributions



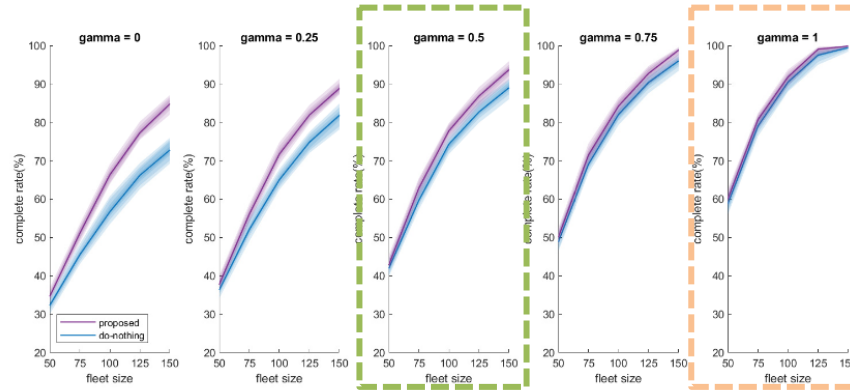
$$p'_d(q) = \gamma \cdot p_d(q) + (1 - \gamma) \cdot p'_o(q)$$

where p'_o is an artificial distribution which has the maximum difference from the origin distribution

- When $\gamma = 1$, the generated destination distribution is equal to the original destination distribution.
- The smaller the γ is, the more discrepancy is introduced between the origin and generated destination distributions.
- When $\gamma = 0$, the generated destination distribution has a shape that is maximally different than the origin one.

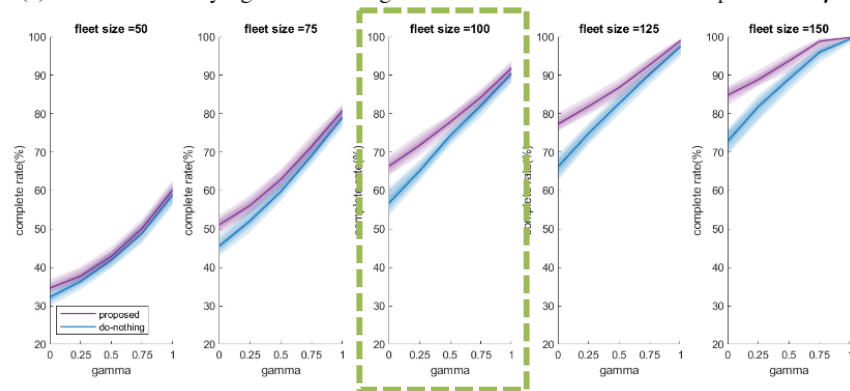
Comparison of performance metrics for various γ and fleet size value

➤ Fleet size



(a) Results with varying values of origin destination demand imbalance parameter γ .

➤ Gamma

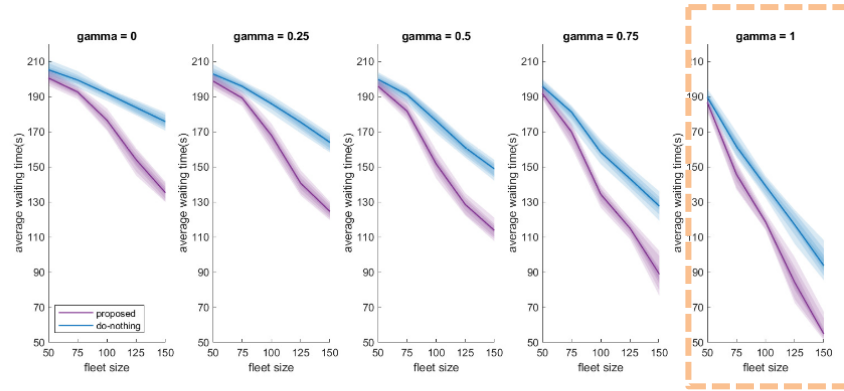


(b) Results with varying values of fleet size.

Completion rate

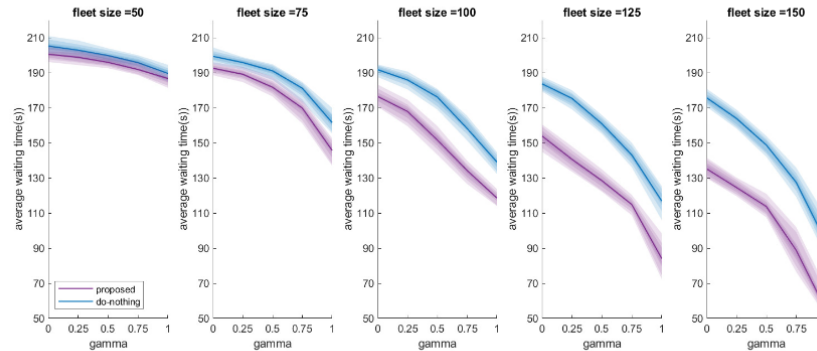
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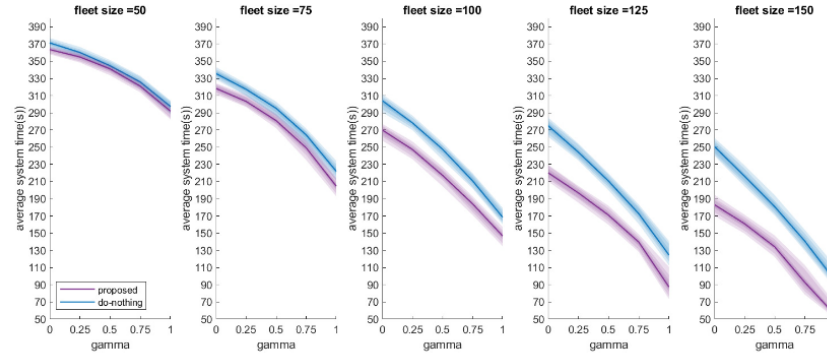


(b) Results with varying values of fleet size.

Average Waiting time

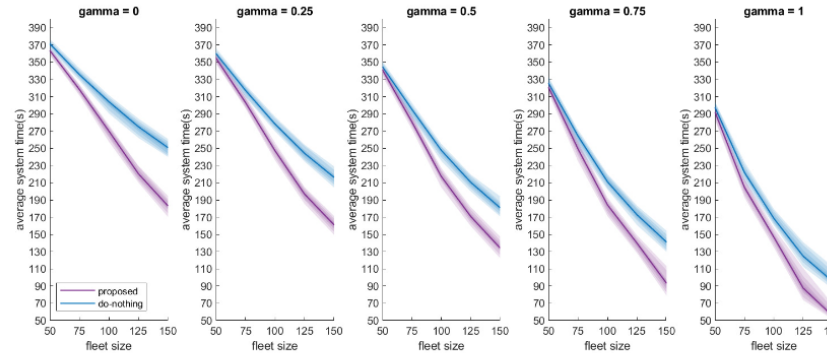
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➤ Fleet size



(a) Results with varying values of origin destination demand imbalance parameter γ .

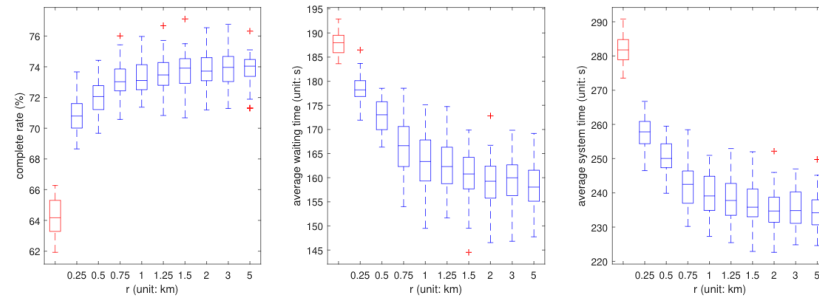
➤ Gamma



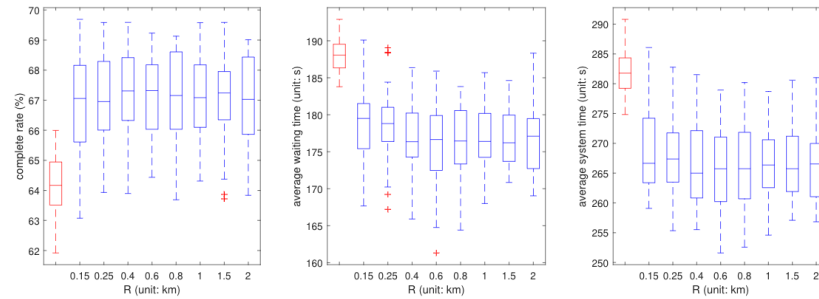
(b) Results with varying values of fleet size.

Average system time

Comparison of performance metrics for various r and R

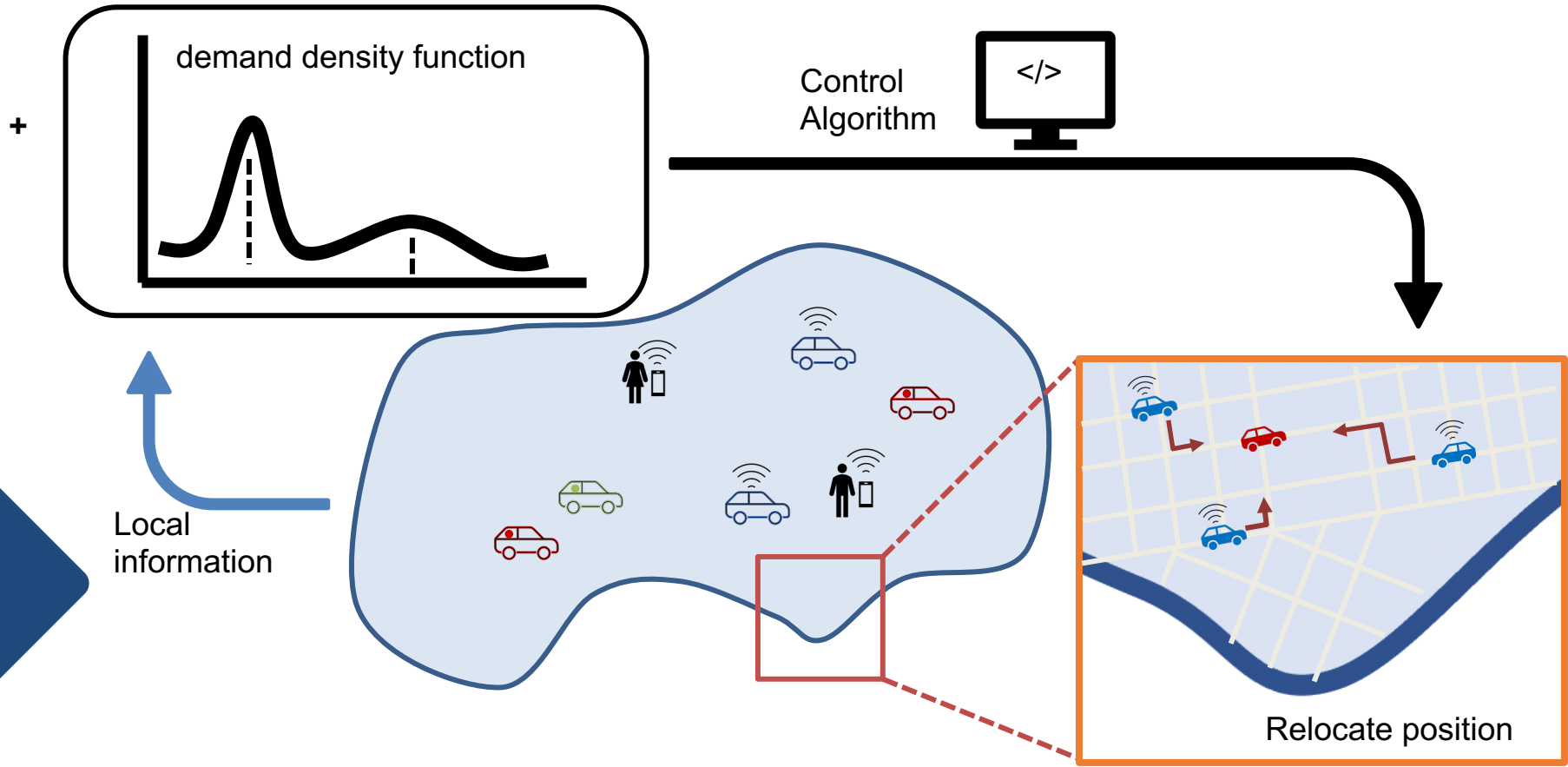


(a) Results with varying values of covering radius r .



(b) Results with varying values of the communication limitation radius R .

Conclusion

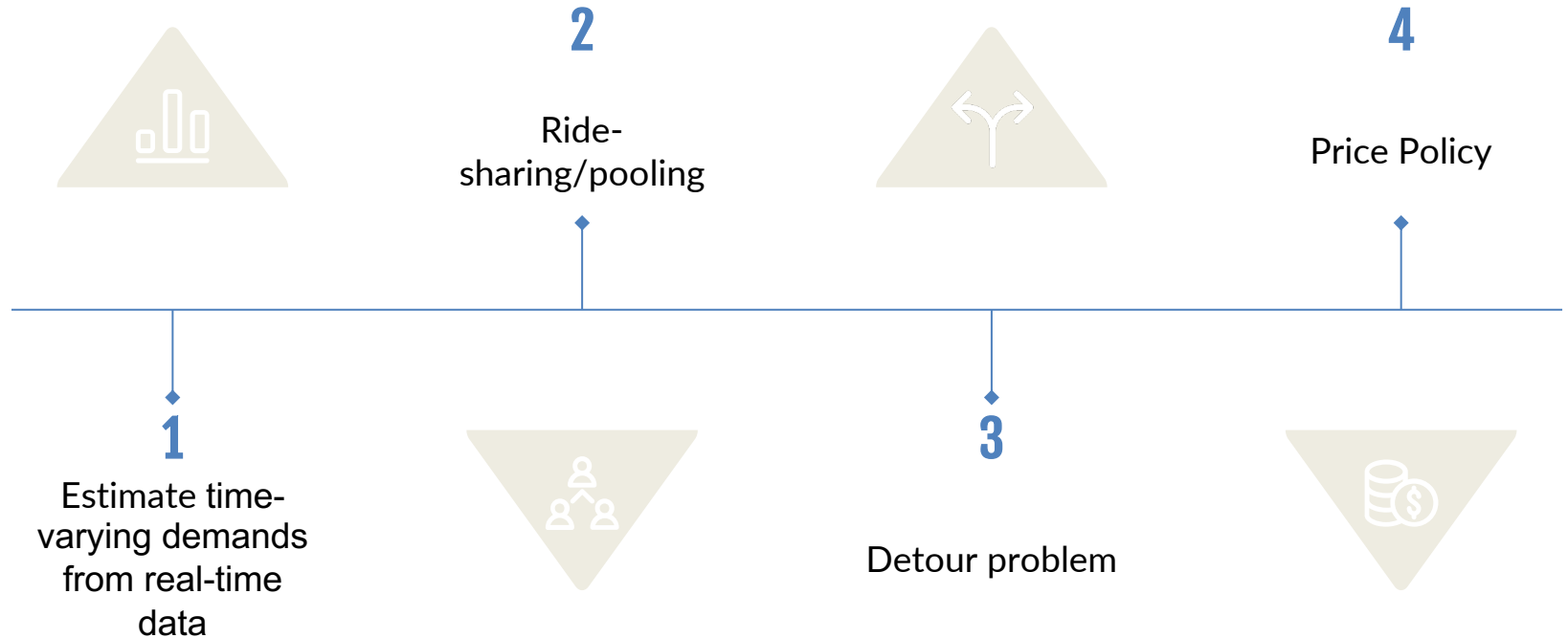


Conclusion

Distributed Coverage Control Algorithm:

- Application to rebalancing of vehicle fleets for urban Mobility-on-Demand systems
- ✓ Countering spatiotemporal imbalances in the origins and destinations of trip demands
- ✓ Dynamically rebalance spatial distribution, serve **more trips** with **less waiting time**.
- ✓ Tested on both continuous and discrete space compared with a do-nothing policy.
- ✓ The effects of coverage and communication radius are demonstrated respectively.

Future steps



Thanks for your attention!

Avez-vous des questions ?

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