## Recent advances in multimodal MFD urban models

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September, 12th, 2021

## Outline

- Macroscopic urban models
- New insights on multimodal MFD from the pNEUMA experiment
- The existing formulations for MFD models
- Multi-reservoir systems and traffic assignment
- Applications of NMFD approaches
- Large-scale simulation of Lyon Metropolis
- Overall assessment of a ride-sharing system
- An optimal route guidance strategy based on avoidance maps
- Trip length calibration and perimeter control


## Introduction to macroscopic urban models

## Transportation models



## Large-scale dynamic urban simulation (1)



## Large-scale dynamic urban simulation (2)



## MFD definition



## Multimodal MFD extension


(a) Production MFD surface.

(b) Velocity MFD surface.

## New insights on multimodal MFD from the pNEUMA experiment

Paipuri, M., Barmpounakis, E., Geroliminis, N., Leclercq, L., 2021. Empirical Observations of Multi-modal Network-level Models: Insights from the pNEUMA Experiment. Transportation Research part C.

## Experimental setting

## $\pi_{\text {neume }}$ \&

## EPFL


https://open-traffic.epfl.ch/


## 2D MFD


(a)

(b)

## Unimodal speed regression



## Multimodal speed regression



## Comparison uni vs. multi regression

| Mode | p-values |  |  |  |  | $v_{f, j}$ |  | $R^{2}$ |  | RMSRE |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Uni- | Multi- |  |  |  |  | Multi- | Uni- | Multi- | Uni- | Multi- |  |
|  | $n_{m}$ | $n_{c}$ | $n_{t}$ | $n_{b}$ | $n_{m}$ | $n_{p}$ |  |  |  |  |  |  |
| Car | 0.01 | 0.01 | 0 | 0 | 0.60 | 0 | 4.06 | 4.06 | 0.01 | 0.75 | 0.125 | 0.065 |
| Taxi | 0 | 0.80 | 0 | 0 | 0.72 | 0 | 4.05 | 4.05 | 0.60 | 0.68 | 0.071 | 0.063 |
| Bus | 0 | 0.14 | 0 | 0 | 0.06 | 0.48 | 2.79 | 2.79 | 0.15 | 0.30 | 0.123 | 0.112 |
| MV | 0 | 0.01 | 0 | 0 | 0.12 | 0.07 | 3.66 | 3.66 | 0.19 | 0.43 | 0.114 | 0.098 |
| PTW | 0 | 0 | 0.06 | 0 | 0.63 | 0 | 4.90 | 4.90 | 0.04 | 0.78 | 0.074 | 0.071 |

## The multimodal two-fluid model

$$
\begin{array}{cl}
\text { Running speed } & v_{r}=v_{f, r}\left(f_{r}\right)^{\check{n}} \equiv v_{f, r}\left(1-f_{s}\right)^{\check{n}}, \\
\text { Mean speed } & v=v_{f, r}\left(f_{r}\right)^{\check{n}+1} \equiv v_{f, r}\left(1-f_{s}\right)^{\check{n}+1} .
\end{array}
$$

Fraction of vehicles that are stopped during a given time internal, i.e., $\quad f_{s}=\frac{T_{s}}{T}$,
The mean stoped time $/ \mathrm{m}$ over the mean travel time $/ \mathrm{m}$
(Herman and Prigogine, 1979)

## The multimodal counterpart

$$
\begin{gathered}
v_{r, j}=v_{f, r, j} \prod_{k \in \mathscr{M}}\left(1-f_{s, k}\right)^{\check{n}_{k, j}}, \forall j \in \mathscr{M} \text { and } \mathscr{M}=\{c, t, b, m, p\}, \\
v_{j}=v_{f, r, j}\left(1-f_{s, j}\right) \prod_{k \in \mathscr{M}}\left(1-f_{s, k}\right)^{\check{n}_{k, j}}, \forall j \in \mathscr{M} \text { and } \mathscr{M}=\{c, t, b, m, p\} .
\end{gathered}
$$

## The Uni two-fluid model


(a)

(b)

(c)

(d)

(e)

## The Multi two-fluid model



## Estimating fs - ergodicity assumption

Weak ergodicity (based on probe sampling) $\quad \hat{f}_{s}=\frac{\bar{T}_{s}}{\bar{T}}$,
Strong ergodicity (based on probe sampling) $\quad \tilde{f}_{s}=\left\langle\frac{T_{S}}{T}\right\rangle$. (Ardekani, 1984)

(a)

(b)

(c)



## The existing formulations for MFD models

Mariotte, G., Leclercq, L., 2019. Flow exchanges in multi-reservoir systems with spillbacks. Transportation Research part B, 122, 327-349.

Mariotte, G., Leclercq, L., Laval, J.A., 2017. Macroscopic urban dynamics: Analytical and numerical comparisons of existing models. Transportation Research Part B,


## The single reservoir setting

Classical dynamic approach


Reservoir (NMFD) approach


## The accumulation-based (bathtub) model



The outflow-MFD is hard to calibrate in practice this is why the steady-state approximation is used

$$
q_{\text {out }}(t)=\frac{Q(n(t))}{L_{\text {trip }}}
$$

## Wave propagation in a single reservoir



## Trip-based model


$\int_{t-T\left(N_{\text {out }}(t)\right)}^{t} V(n(s)) d s=L$
(Arnott, 2013)
(Lamotte \& Geroliminis, 2016)
$T\left(N_{\text {out }}(t)\right)$ : experimented travel time for vehicle $N_{\text {out }}$ that exits at time $t$
$\Leftrightarrow Q_{\text {out }}(t)=\frac{Q_{\text {in }}\left(t-T\left(N_{\text {out }}(t)\right)\right) V(n(t))}{\left.V\left(n\left(t-\underline{T\left(N_{\text {out }}(t)\right.}\right)\right)\right)}$
(Delay differential equation with endogenous delay)
$Q_{\text {out }}(t)=Q_{\text {in }}(t)+n^{\prime}(t)$
(Accumulation-based MNFD model)





## Trip-based model (2)



An event-based numerical scheme

## Advantages

- Direct access to entry and exit times for all individual vehicles
- Efficient numerical scheme as only the next vehicle to exit should be updated in practice at each event
- Straightforward extension to account for heterogeneous travel distances


## Multimodal extensions

- Accumulation-based version

$$
\frac{d n_{i}(t)}{d t}=q_{\text {in }, i}(t)-q_{\text {out }, i}(t) \text { with } q_{\text {out }, i}(t)=\frac{n_{i}}{n} \frac{P\left(n_{i} \ldots\right)}{L_{i}}
$$

- Trip-based version

$$
L_{c, r}=\int_{t-\tau_{c, r}(t)}^{t} v_{c, r}\left(n_{c, r}(s), n_{p, r}(s)\right) \mathrm{d} s,
$$

- Accumulation-based version with delay

$$
\int_{-\infty}^{t} q_{m, \text { in }}(s) \mathrm{d} s=\int_{-\infty}^{t+\tau_{m}(t)} q_{m, \text { out }}(s) \mathrm{d} s . \quad \quad q_{m, \text { out }}\left(t+\tau_{m}(t)\right)=\frac{q_{m, \text { in }}(t)}{1+\frac{\mathrm{d} \tau_{m}(t)}{\mathrm{d} t}}
$$

It requires stabilization when inflow decreases

## Comparison of multimodal MFD extensions



Single 3D MFD

(a) Accumulation $v s$. time for cars.


(b) Accumulation vs. time for buses.

(d) Outflow vs. time for buses.

## Comparison of multimodal MFD extensions

Segragated 3D MFD

(a) Accumulation vs. time for cars.

(c) Outflow vs. time for cars

(b) Accumulation $v s$. time for buses

(d) Outflow vs. time for buses

## Multi-reservoir systems and traffic assignment

Batista, S., Leclercq, L., Menendez, M., 2021. Dynamic traffic assignment for regional networks with traffic-dependent trip lengths and regional paths. Transportation Research part C,

Batista, S.F.A., Leclercq, L., 2019. Regional dynamic traffic assignment framework for MFD multi-regions models. Transportation Science,

## Multi-reservoir systems



## Estimation of the trip lengths



## Impacts on the simulation results



Time-evolution of the accumulation

## Trip lengths estimation - cellphone data



LBS data over Dallas city (US) - 6 months


Paipuri, M., Xu, Y., Gonzalez, M.C., Leclercq, L., 2020. Estimating MFDs, Trip Lengths and Path Flow Distributions in a Multi-region Setting Using Mobile Phone

## Application to the Lyon Metropolis

Mariotte, G., Leclercq, L., Batista, S.F.A., Krug, J., Paipuri, M., 2020. Calibration and validation of multi-reservoir MFD models: A case study in Lyon. Transportation Research part B.

MFDUrbaSim (A python open-source MFD simulator): https://github.com/licit-lab/MFDurbanSim

## MFD simulation for Lyon metropolis



## Demand estimation



## The 1-reservoir case



## The 5-reservoir case - user equilibrium

Gap $=4.9$
$3 \%$ of OD with a Gap ${ }^{o d}>0.2$







## The 5-reservoir case - best fit

Gap $=5.4$
$7 \%$ of OD with a Gapod $>0.2$







## The 10-reservoir case - best fit

Gap $=61$
31 \% of OD with a Gap ${ }^{o d}>0.2$


## Assessing ride-sharing services

Alisoltani, N., Leclercq, L., Zargayouna, M., 2021. Can dynamic ride-sharing reduce traffic congestion? Transportation Research part B.

## Test Case - Northern Lyon

## Test cases

Lyon 6 + Villeurbanne
Scale of $25 \mathrm{~km}^{2}$ 62450 requests
11235 Service requests
1,883 nodes and 3383 links
6:30 to 10:30 AM (morning peak)
Rolling horizon: 20 min
Optimization time step: 10 min


## Test case - Full Lyon

## Test cases

Lyon

Scale of $80 \mathrm{~km}^{2}$
484,690 requests
205,308 Service requests
11,314 origin/destination set points
6 to 10 AM (morning peak)
Rolling horizon: 20 min
Optimization time step: 10 min



## Traffic dynamics for different market share

## Northern Lyon



Increase in travel time
Market-share 100\%: 5.5\%
Market-share 80\%: 4.4\%
Market-share 60\%: 3.3\%

Market-share 40\%: 2.3\%
Market-share 20\%: 1.1\%

Traffic situation for the number of sharing 0 with different market-shares

## Traffic dynamics for different sharing level



## Application to full Lyon Metropolis (1)



## Application to full Lyon Metropolis (2)

Full Lyon


## Application to full Lyon Metropolis (3)

| Number of <br> sharing | Number of trips | Number of cars |
| :--- | :--- | :--- |
| 0 | 205124 | 17102 |
| 1 | 105745 | 9489 |
| 2 | 72160 | 6826 |
| 3 | 69790 | 6595 |

## Impact of dynamic ride-sharing on large-scale network

Market-share


Total travel distance for all the cars for the number of sharing 0,1 and 2 with different market-shares

## Impact of dynamic ride-sharing on large-scale network

## Capacity of vehicles

Regular vehicle: capacity $=4$, nshare $=3$
Big vehicle: capacity $=6$, nshare $=5$
Van-pooling: capacity $=10$, nshare $=9$
Shuttle-sharing: capacity $=20$, nshare $=19$

| Coniguration | Shared vehicles |  |
| :--- | :---: | :---: |
|  | Number of trips | Number of <br> cars |
| MS: $100 \%$ |  |  |
| Capacity $=4$ | 69790 | 6595 |
| Capacity $=6$ | 63304 | 5714 |
| Capacity $=10$ | 46448 | 4253 |
| Capacity $=20$ | 30004 | 2785 |



Traffic situation for different vehicle capacity (market-share $=\mathbf{1 0 0 \%}$ )

## An optimal route guidance strategy based on avoidance maps

## Route guidance based on avoidance maps


(b)

(c)


## Assessment on a toy network



## Assessment on a real network



Special thanks to the MAGnUM team!

## Thank you for your attention



